

Resonance Review

$\Delta L = \frac{1}{2}\lambda$ $\Delta L = \frac{1}{2}\lambda$
 $L_1 = \frac{1}{2}\lambda$ $L_2 = \frac{3}{2}\lambda$ $L_3 = \frac{5}{2}\lambda$

open
 closed

Shortest tube: $L_1 = \frac{1}{2}\lambda$
 Spacing: $\Delta L = \frac{1}{2}\lambda$
 $L_n = n \frac{\lambda}{2}$ $f_n = n f_1$

Shortest tube: $L_1 = \frac{1}{4}\lambda$
 Spacing: $\Delta L = \frac{1}{2}\lambda$
 $L_n = (2n-1) \frac{\lambda}{4}$ $f_n = (2n-1) f_1$

$\Delta L = \frac{1}{2}\lambda$ $\Delta L = \frac{1}{2}\lambda$
 (spacing)

mp|425

open

$f_1 = 330\text{Hz}$

a) f_2 and $f_3 = ?$

b) $L_1 = ?$ if $v = 344\text{m/s}$

a) $f_n = n f_1$

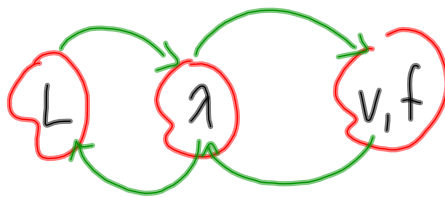
$f_2 = 2 f_1$

$f_2 = 2(330\text{Hz})$

$f_2 = 660\text{Hz}$

$f_3 = 3(330\text{Hz})$

$f_3 = 990\text{Hz}$



b) $v = \lambda f$

$\lambda = \frac{v}{f}$

$\lambda = \frac{344\text{m/s}}{330/\text{s}}$

$\lambda = 1.04\text{m}$

$L_1 = \frac{1}{2}\lambda$

$L_1 = \frac{1}{2}(1.04\text{m})$

$L_1 = 0.520\text{m}$

MP1426

closed

$$f_1 = 330 \text{ Hz}$$

$$L_1 = ?$$

$$v = 344 \text{ m/s}$$

$$\lambda = 1.04 \text{ m (from last question)}$$

$$L_1 = \frac{1}{4} \lambda$$

$$L_1 = \frac{1}{4} (1.04 \text{ m})$$

$$L_1 = 0.260 \text{ m}$$

$$f_2 \text{ and } f_3 = ?$$

$$f_n = (2n-1)f_1$$

$$f_3 = (2(3)-1) 330 \text{ Hz}$$

$$f_2 = (2(2)-1) 330 \text{ Hz}$$

$$f_3 = (5)(330 \text{ Hz})$$

$$f_2 = (3)(330 \text{ Hz})$$

$$f_3 = 1650 \text{ Hz}$$

$$f_2 = 990 \text{ Hz}$$

Use the spacing in our demo to figure out the speed of sound.

$$L_2 = 24.5 \text{ cm}$$

$$L_3 = 42.5 \text{ cm}$$

2 successive resonance lengths

$$\Delta L = 42.5 \text{ cm} - 24.5 \text{ cm}$$

$$\Delta L = 18.0 \text{ cm}$$

$$\uparrow \frac{1}{2} \lambda$$

$$\therefore \Delta L = \frac{1}{2} \lambda$$

$$18.0 \text{ cm} = \frac{1}{2} \lambda$$

$$\lambda = 36.0 \text{ cm}$$

$$v = \lambda f$$

$$v = (0.360 \text{ m})(1000 \text{ Hz})$$

$$v = 360 \text{ m/s}$$

$$v = 331 + 0.59 T$$

$$360 \text{ m/s} = 331 \text{ m/s} + (0.59 \frac{\text{m/s}}{^\circ\text{C}}) T$$

$$29 \text{ m/s} = (0.59 \frac{\text{m/s}}{^\circ\text{C}}) T$$

$$T = \frac{29 \text{ m/s}}{0.59 \text{ m/s}/^\circ\text{C}}$$

$$T = 49^\circ\text{C} \leftarrow \text{HOT!}$$